

SEC 4 TS

Systems of Equations Review March 2017

Comparison Method

What to do?

EXAMPLES

a) $4x + y = 2$
 $x - y = 3$

$$\begin{aligned}y &= -4x + 2 \\y &= x - 3 \\-4x + 2 &= x - 3\end{aligned}$$

$$-5x = -5$$

$$x = 1$$

$$y = 1 - 3$$

$$y = -2$$

$$(1, -2)$$

b) $x + 7y = 0$
 $2x - 8y = 22$

$$\begin{aligned}y &= -\frac{x}{7} \\y &= \frac{1}{4}x - \frac{11}{4}\end{aligned}$$

$$\frac{-x}{7} = \frac{1}{4}x - \frac{11}{4}$$

$$\frac{-11}{28}x = \frac{11}{4}$$

$$x = -7$$

$$y = 1$$

$$(-7, 1)$$

c) $-7x + 2y = 18$
 $6x + 6y = 0$

$$y = \frac{7}{2}x + 9$$

$$y = -x$$

$$\frac{7}{2}x + 9 = -x$$

$$\frac{9}{2}x = -9$$

$$x = -2$$

$$y = 2$$

$$(-2, 2)$$

d) $4x - y = 20$
 $-2x - 2y = 10$

$$y = 4x - 20$$

$$y = -x - 5$$

$$4x - 20 = -x - 5$$

$$5x = 15$$

$$x = 3$$

$$y = -8$$

$$(3, -8)$$

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Substitution Method

What to do?

EXAMPLES

a) $3x - 5y = 17$
 $y = -7$

$$3x - 5(-7) = 17$$

$$3x + 35 = 17$$

$$3x = -18$$

$$x = -6$$

$$y = -7$$

$$(-6, -7)$$

b) $y = -5$
 $5x + 4y = -20$

$$5x + 4(-5) = -20$$

$$5x - 20 = -20$$

$$5x = 0$$

$$x = 0$$

$$y = -5$$

$$(0, -5)$$

c) $7x + 2y = -19$
 $-x + 2y = 21$

$$x = 2y - 21$$

$$7(2y - 21) + 2y = -19$$

$$14y - 147 + 2y = -19$$

$$12y = 128$$

$$y = \frac{32}{3}$$

$$x = 2\left(\frac{32}{3}\right) - 21$$

$$x = \frac{1}{3}$$

$$\left(\frac{1}{3}, \frac{32}{3}\right)$$

d) $6x + 8y = -22$
 $y = -5$

$$6x + 8(-5) = -22$$

$$6x - 40 = -22$$

$$6x = 18$$

$$x = 3$$

$$y = -5$$

$$(3, -5)$$

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Elimination Method

What to do?

EXAMPLES

a) $8x - 6y = -20 \quad (-16)$
 $-16x + 7y = 30 \quad (8)$

$$\begin{array}{r} -128x + 96y = 320 \\ -128x + 56y = 240 \\ \hline 40y = 80 \end{array}$$

$$\begin{aligned} y &= 2 \\ 8x - 12 &= -20 \\ 8x &= -8 \\ x &= -1 \\ (-1, 2) \end{aligned}$$

c) $-16 + 20x - 8y = 0 \quad (-18)$
 $-18y - 22x = 36 \quad (-8)$

$$\begin{array}{r} 288 - 360x + 144y = 0 \\ 144y + 176x = -288 \end{array}$$

$$\begin{array}{r} 288 - 360x + 144y = 0 \\ 288 + 176x + 144y = 0 \\ \hline -536x = 0 \end{array}$$

$$x = 0$$

$$\begin{aligned} 288 + 176(0) + 144y &= 0 \\ 144y &= -288 \\ y &= -2 \end{aligned}$$

$$(0, -2)$$

b) $-8x - 10y = 24 \quad (6)$
 $6x + 5y = 2 \quad (-8)$

$$\begin{array}{r} -48x - 60y = 144 \\ -48x - 40y = -16 \\ \hline -20y = 160 \end{array}$$

$$\begin{aligned} y &= -8 \\ 6x + 5(-8) &= 2 \\ 6x - 40 &= 2 \\ 6x &= 42 \end{aligned}$$

$$x = 7 \quad (7, -8)$$

d) $-16y = 22 + 6x \quad (-11)$
 $-11y - 4x = 15 \quad (-16)$

$$\begin{array}{r} -16y - 6x = 22 \\ -11y - 4x = 15 \\ \hline -55y - 10x = 37 \end{array}$$

$$\begin{array}{r} 176y + 66x = -242 \\ 176y + 64x = -240 \\ \hline 2x = -2 \end{array}$$

$$\begin{aligned} x &= -1 \\ -16y - 4(-1) &= 15 \\ -16y &= 11 \end{aligned}$$

$$-16y = 22 + 6(-1)$$

$$-16y = 16$$

$$y = -1$$

$$(-1, -1)$$

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PRACTICE WORD PROBLEMS

Two tables at a restaurant receive their bills shown below. How much more does an adult pay compared to a child? If a party of 12 adults and 18 children sat down, how much would the bill total?

Table 1:
6 adults
4 kids
\$ 97

Table 2:
5 kids
3 adults
\$ 65

$x = \text{adult}$

$y = \text{Kid}$

Table 1

$$6x + 4y = 97$$

Table 2

$$3x + 5y = 65$$

$$6x + 4y = 97 \quad (3)$$

$$3x + 5y = 65 \quad (6)$$

$$\begin{array}{r} 18x + 12y = 291 \\ 18x + 30y = 390 \\ \hline -18y = -99 \end{array}$$

$$y = 5.50$$

$$6x + 4(5.50) = 97$$

$$6x = 75$$

$$x = 12.50$$

$$(12.50, 5.50)$$

$$\begin{aligned} 12(12.5) + 18(5.50) \\ = 249 \$ \end{aligned}$$

Difference between adult and child is 7\$.